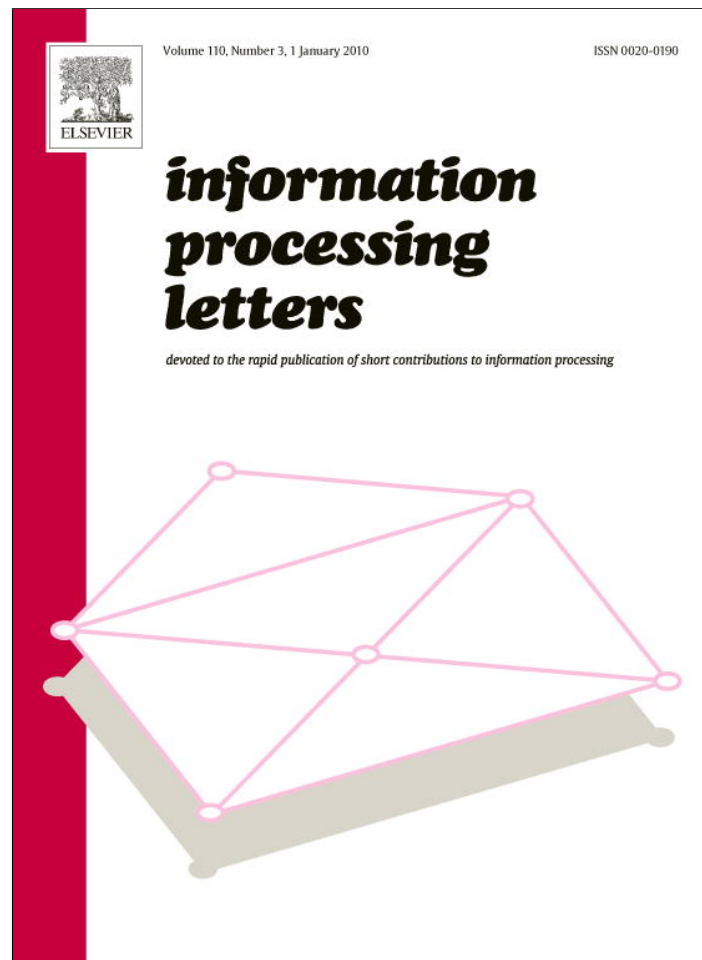


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A network flow based approach for network selection in dynamic spectrum access networks

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ABSTRACT

In this paper, we present a network flow based approach for dynamic network and channel selection for secondary users in dynamic spectrum access networks. Most approaches in the current literature on dynamic spectrum access networks do not consider dynamic network and channel selection. We present a network flow framework for network selection. We show that our approach can enable re-assignment of networks to secondary users and also re-assignment of channels to secondary users within the same network. The assignments and re-assignments take into account, the interference caused to primary users, the price each secondary user is willing to pay and the quality of service (QoS) obtained by each secondary user. We obtain a bound for the maximum number of re-assignments.

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1. Introduction

The developments in software defined radio (SDR), dynamic spectrum access (DSA) and cognitive radio networks resulted in the paradigm of users sharing spectrums on an opportunistic basis. Users belonging to one network sense spectrum opportunities in another network and contend for the unused spectrum in this second network. The users thereby become “secondary” users in the second network. Users that originally subscribed to the second network are called “primary users.” The combined interference caused by all secondary users to existing primary users should be below a specified threshold. A comprehensive survey of cognitive radio networks and dynamic spectrum access networks is presented in [1].

Resource allocation in cognitive radio networks has been studied with different approaches like graph theoretic models [2], game theoretic models [3,4] and learning automata [5]. Spectrum assignment for cognitive radio networks based on graph coloring approaches was studied in [2]. The authors provide heuristics for different fairness

criteria and evaluate them. In [3], Larcher et al. present an n player non-cooperative game theoretic approach for secondary user spectrum access. A utility function based on the access delay and collision probability was proposed, and the existence and convergence to a Nash equilibrium was shown. In [4], Xing et al. presented the homo-equalis game theoretic model for secondary user spectrum access in which users were modeled to behave like a human society to reduce the unfairness in spectrum access. In [5], Xing et al. presented a learning automata based approach where users were classified as quality sensitive and price sensitive users and the price dynamics were studied.

Most approaches in the literature however did not consider allocation of secondary users to networks and also did not consider dynamic re-assignment of the available channels to secondary users and dynamic re-assignment of secondary users to the different available networks. Users¹ can choose networks based on several factors that include signal strength, quality-of-service (QoS) and price. Also, dynamic re-assignment of users to different networks or different channels in the same network based on the channel

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¹ Henceforth, throughout the paper, whenever we mention “users,” we mean “secondary users” unless explicitly mentioned otherwise.

and interference conditions could result in a better spectrum utilization. In this paper, we apply the theory of multi-commodity network flows [6] to determine an optimal allocation of users to networks based on factors like QoS, interference thresholds on primary users and price. We show that our approach can enable re-assignment of networks to secondary users and also re-assignment of channels to secondary users within the same network. We also determine the maximum number of re-assignments in the network.

2. System model

Our objective is to obtain a framework to allocate secondary users to different available networks. Each user i enters the system with a minimum rate requirement and is willing to pay a maximum price. There are n networks and each network contains a specified number of channels that can be used by a secondary user. Any secondary user, when allocated a channel in a network, transmits with a fixed power and causes interference to the primary users in the network. The amount of interference caused depends on the location of the user and the channel conditions on the channel. It is desired to limit the maximum interference to the primary users below a specified threshold. Users are to be assigned to networks to satisfy all the above constraints. We make the following assumptions:

- There are M users m_1, m_2, \dots, m_M and n networks, S_1, S_2, \dots, S_n in the system.
- The i th user in the system has a minimum rate requirement r_i^{\min} .
- The i th user in the system can pay a maximum price p_i^{\max} .
- Network S_k contains N_k channels, $f_{1k}, f_{2k}, \dots, f_{N_k k}$, available for transmission. $F \triangleq \sum_{k=1}^n N_k$.
- The users m_1, m_2, \dots, m_M are all secondary users to networks S_1, S_2, \dots, S_n . In other words, the networks to which $m_1 \dots m_M$ are primary users, are distinct from $S_1 \dots S_n$.
- A user m_i who is assigned channel f_{jk} in network S_k causes a maximum of h_{jk} units of interference to a primary user in the network S_k .
- In any network S_k , a channel f_{jk} can be assigned to at most one user.
- In any network S_k , the maximum tolerable interference to any primary user on channel f_{jk} is ϵ_{jk} .
- In any network S_k , the maximum possible rate of transmission on channel f_{jk} is R_{jk}^{\max} . The value of R_{jk} depends on the channel conditions of channel j in network k .
- There is a centralized controller in the network which obtains the required parameters from all the secondary users in the network.²

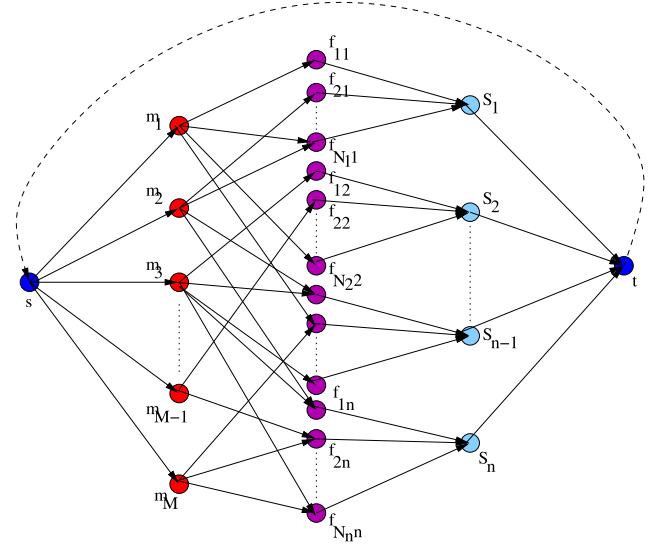


Fig. 1. A network graph representation of cognitive radio systems.

3. Network flow formulation

The network graph representation of a cognitive radio system is as shown in Fig. 1. In Fig. 1, node m_i , $1 \leq i \leq M$, represents the i th user, node f_{jk} denotes the j th channel in the k th network and node S_k denotes the k th network. Nodes s and t denote dummy source and sink nodes, respectively.

A directed edge (s, m_i) exists to all users. A directed edge (m_i, f_{jk}) exists if user m_i can use channel f_{jk} , i.e., user m_i senses channel f_{jk} to be available. A directed edge (f_{jl}, S_k) exists if and only if $l = k$. Edges (S_k, t) exists $\forall k$. Finally, there is a dummy directed edge from t to s , which translates the minimum cost flow problem to the flow maximization problem.

Along any edge e , the flow on the edge is represented as $[x_e^1 \ x_e^2 \ x_e^3 \ x_e^4]$. x_e^1 denotes the price parameter on the edge, x_e^2 denotes the interference parameter, x_e^3 denotes the rate of transmission, and x_e^4 denotes usage of a particular channel in a network. For edges e of the form (s, m_i) , the flow term x_e^1 denotes the price paid by user m_i . For any edge e of the form (m_i, f_{jk}) , x_e^2 denotes the interference caused by user m_i to a primary user in network S_k on channel f_{jk} , and x_e^3 denotes the rate at which user m_i transmits on channel f_{jk} in network S_k . For any edge e of the form (f_{jk}, S_k) , the flow term x_e^2 denotes the total interference experienced by a primary user on channel f_{jk} in network S_k , and $x_e^4 = 0$ if channel f_{jk} is not assigned to any user in network S_k and $x_e^4 = 1$ otherwise.

Capacities of any edge e is of the form $[u_e^1 \ u_e^2 \ u_e^3 \ u_e^4]$. From the system model described in Section 2, the capacities of edges are obtained as follows: For any edge e of the form (s, m_i) , $u_e^1 = p_i^{\max}$, and $u_e^2 = u_e^3 = u_e^4 = \infty$. The first capacity parameter denotes the maximum price the user can pay. For any edge e (m_i, f_{jk}) , $u_e^1 = u_e^2 = u_e^3 = u_e^4 = \infty$. For edge (f_{jk}, S_k) , $u_e^1 = \infty$, $u_e^2 = \epsilon_{jk}$, $u_e^3 = R_{jk}^{\max}$, and $u_e^4 = 1$. The capacity parameter $u_e^4 = 1$ ensures that no two users in the same network use the same channel. Finally, for the edge (S_k, t) and the edge $e = (t, s)$, $u_e^1 = u_e^2 = u_e^3 = u_e^4 = \infty$. Each edge e also has a lower

² The parameters can be obtained directly from the secondary users or from the networks. The exact protocol to obtain the information is beyond the scope of this paper.

bound of the form $[l_e^1 \ l_e^2 \ l_e^3 \ l_e^4]$. From the system model described in Section 2, for edges of the form $e = (s, m_i)$, $l_e^3 = r_i^{\min}$, $l_e^L = 0$, $L = 1, 2, 4$. For $e \neq (s, m_i)$, $l_e^L = 0$, $L = 1, 2, 3, 4$.

Associated with each edge e is a cost vector of the form $C_e = [C_e^1 \ C_e^2 \ C_e^3 \ C_e^4]$. For every directed edge $e = (x, y)$ in the graph, if $\bar{e} \triangleq (y, x)$, then $C_{\bar{e}}^L = -C_e^L$, $L = 1, 2, 3, 4$. For the edge $e = (t, s)$, $C_e^L \leq 0$, $L = 1, 2, 3, 4$.

Let $\phi_L \in [0, 1]$, be the weight given to flow parameter L , $L = 1, 2, 3, 4$, and let $\sum_{L=1}^4 \phi_L = 1$. The weights ϕ_L are statically assigned to the parameters corresponding to different users. The weights denote the priorities assigned to different criteria. As an example, $\phi_1 = 1$ and $\phi_2 = \phi_3 = \phi_4 = 0$ represents a scenario where users like to choose the network purely on the basis of price alone and do not take QoS or interference into account while choosing the network.

The network selection problem for secondary users can then be formulated as the following optimization problem:

$$\text{Minimize } \sum_{L=1}^4 \sum_{e \in A} \phi_L C_e^L x_e^L \quad (1)$$

subject to

$$l_e^L \leq x_e^L \leq u_e^L, \quad \forall e \in A, \ L = 1, 2, 3, 4, \quad (2)$$

and

$$\sum_{j: (i,j) \in A} x_{ij}^L - \sum_{j: (j,i) \in A} x_{ji}^L = 0, \quad \forall i \in N, \ L = 1, 2, 3, 4. \quad (3)$$

The above optimization problem is the multi-commodity minimum cost flow problem [6] without the bundle constraints. When a new user enters the system, the graph is modified to include the new user (if the new user can be admitted) and the minimum cost flow problem is solved for the new graph which includes the new user. The following theorem specifies the necessary and sufficient condition for admitting new users.

Theorem 3.1. *A newly arriving secondary user m_i can be assigned a channel on a network and hence be admitted if and only if there exists a flow augmenting directed path from s to t which includes m_i .*

Proof. Let there be a flow augmenting path $s \rightarrow m_i \rightarrow f_{jk} \rightarrow S_k \rightarrow t$ directed from s to t . Since the specified path is a flow augmenting path, it satisfies the constraints (2) and (3). The path also indicates that user m_i can use channel f_{jk} in network S_k . Hence assignment of channel f_{jk} (in network S_k) to the user m_i is a feasible assignment.

Consider a new user m_i that has arrived but there is no flow augmenting path from s to t through m_i . This indicates that all paths from s to t through m_i have at least one saturated edge. This implies that it is not possible to assign any of the available channels in any of the networks to m_i . This is because, such an assignment would result in an increase in the flow parameters corresponding to edges

of the form (m_i, f_{jk}) for some j and k , thus resulting in violation of constraints (2). Therefore, m_i cannot be admitted in the system. Therefore, for m_i to be admitted, a flow augmenting path is essential. \square

Due to changes in channel conditions and the location of the users, they can be re-assigned channels in the same network or re-assigned to different networks. User m_i currently assigned channel f_{jk} in network S_k can be re-assigned to a) channel $f_{j'k}$ in network S_k or b) to channel $f_{j''k'}$ in network $S_{k'}$. In case a), the re-assignment is equivalent to reducing the flows on edges of the form (m_i, f_{jk}) and (f_{jk}, S_k) , and increasing the flows on edges of the form $(m_i, f_{j'k})$ and $(f_{j'k}, S_k)$. In case b), the re-assignment is equivalent to reducing the flows on edges of the form (m_i, f_{jk}) and (f_{jk}, S_k) , and increasing the flows on edges of the form $(m_i, f_{j''k'})$ and $(f_{j''k'}, S_{k'})$. However, there could be multiple re-assignments. For example, consider a user m_i using channel f_{jk} on network S_k and another user $m_{i'}$ using channel $f_{j'k}$ in network S_k . If user $m_{i'}$ is re-assigned some other channel $f_{j''k'}$ in network $S_{k'}$, then channel $f_{j'k}$ also becomes available for use to user m_i . This re-assignment results in the undirected path $s - m_i - f_{jk} - S_k - f_{j'k} - m_{i'} - f_{j''k'} - S_{k'} - t$ along which flows are augmented. It is noted that directed edges of the form $(S_k, f_{j'k})$ and $(f_{j'k}, m_{i'})$ do not exist in the graph and hence flows and costs on these edges would be negative.

Since re-assignments involve additional costs, it is of interest to compute the number of re-assignments possible. The following lemma and theorem provide a bound on the number of re-assignments.

Lemma 3.1. *Consider the flow vector \underline{x}^L ($L = 1, 2, 3, 4$).³ Let \underline{x}^{*L} be the optimal flow vector for commodity L . $\underline{x}^{*L} - \underline{x}^L$ can be decomposed into at most $|A|$ number of negative cost directed cycles, where $|A|$ is the number of edges in the network.*

Proof. Consider any feasible flow vector, \underline{x}^L , and the optimal flow vector, \underline{x}^{*L} . The optimal flow vector is obtained from the feasible flow vector by saturating unsaturated edges. Also, to satisfy flow conservation constraints, it is essential to find a negative cost directed cycle and modify the flow by the same amount on all edges on the cycle. Hence \underline{x}^{*L} can be obtained from \underline{x}^L by a sequence of identifying negative cost directed cycles and saturating at least one edge in each cycle. The flow $\underline{x}^{*L} - \underline{x}^L$ can be looked upon as a feasible flow in the residual graphs, which can also be decomposed into a sequence of negative cost directed cycles saturating at least one edge at a time. Since there are $|A|$ number of edges, the flow $\underline{x}^{*L} - \underline{x}^L$ can be decomposed into at most $|A|$ number of negative cost directed cycles. \square

Theorem 3.2. *The maximum number of re-assignments for an L commodity multi-commodity flow problem is $L \lfloor \frac{|A|}{2} \rfloor$.*

Proof. Let the number of negative cost directed cycles for commodity l , $1 \leq l \leq L$, be α_l . It is noted that for the prob-

³ A flow vector \underline{x}_L is the vector of the form $[x_e^L]_{1 \leq e \leq |A|}$.

lem under consideration, a negative cost directed cycle can be of length 4 for an intra-network handoff and of length 6 for an inter-network handoff. If the length is β , then $\beta/2$ number of edges in the cycle correspond to the current channel in the current network for the user and $\beta/2$ number of edges correspond to the new channel and/or the new network. Therefore, only half of a directed cycle can be saturated on each re-assignment. In other words, C_l number of cycles can result in $\lfloor \frac{C_l}{2} \rfloor$ re-assignments. Hence the total number of re-assignments can at most be $\sum_{l=1}^L \lfloor \frac{C_l}{2} \rfloor$, which, from Lemma 3.1, yields $L \lfloor \frac{|A|}{2} \rfloor$ on simplification. \square

From the algorithms specified in Chapter 9 in [6], the complexity of the multi-commodity flow problem for a system with M users, N networks and F channels, can be shown to be $O((M + N + F)^3 \log(M + N + F))$.

4. Conclusion

We presented an L -commodity network flow framework for network selection for secondary users in DSA based cognitive radio networks. We showed that the maximum re-assignments is $L \lfloor \frac{|A|}{2} \rfloor$ for a network with $|A|$ directed edges. Inclusion of transmission power constraints

and convex non-linear objective functions for QoS are topics for further study.

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