

Homework 3 – due 6/2

3-5) Simplify the following Boolean functions, using four-variable maps:

(a) $F(w,x,y,z) = \Sigma(1, 4, 5, 6, 12, 14, 15)$

(b) $F(A,B,C,D) = \Sigma(0,1,2,4,5,7,11,15)$

(c) $F(w,x,y,z) = \Sigma(2,3,10,11,12,13,14,15)$

(d) $F(A,B,C,D) = \Sigma(0,2,4,5,6,7,8,10,13,15)$

a)

wxyz	00	01	11	10
00	0	1	0	0
01	1	1	0	1
11	1	0	1	1
10	0	0	0	0

$$F(w,x,y,z) = w'y'z + xz' + wxy$$

b)

ABCD	00	01	11	10
00	1	1	0	1
01	1	1	1	0
11	0	0	1	0
10	0	0	1	0

$$F(A,B,C,D) = A'C' + A'B'D' + BCD + ACD$$

c)

Wxyz	00	01	11	10
00	0	0	1	1
01	0	0	0	0
11	1	1	1	1
10	0	0	1	1

$F(w,x,y,z) = x'y + wx$

d)

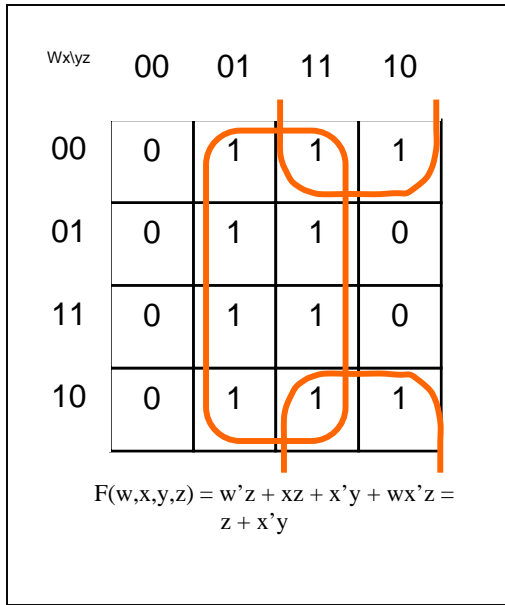
ABCD	00	01	11	10
00	1	0	0	1
01	1	1	1	1
11	0	1	1	0
10	1	0	0	1

$F(A,B,C,D) = B'D' + A'B + BD$

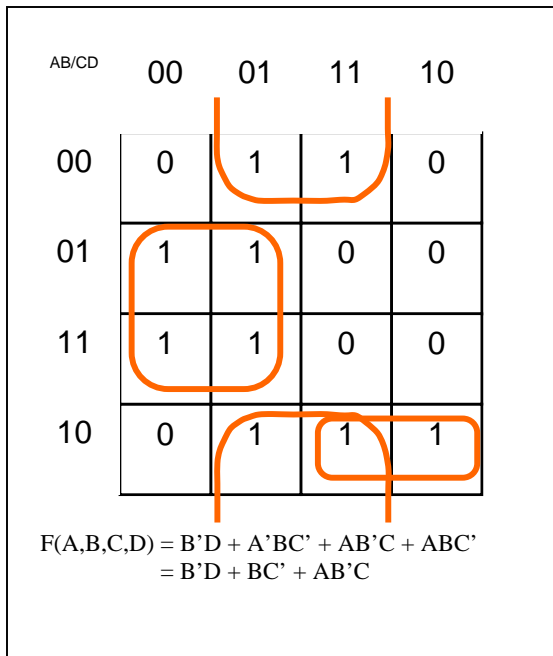
3-7) Simplify the following Boolean expressions, using four-variable maps:

- (a) $w'z + xz + x'y + wx'z$
- (b) $B'D + A'BC' + AB'C + ABC'$
- (c) $AB'C + B'C'D' + BCD + ACD' + A'B'C + A'BC'D$
- (d) $wxy + yz + xy'z' + x'y$

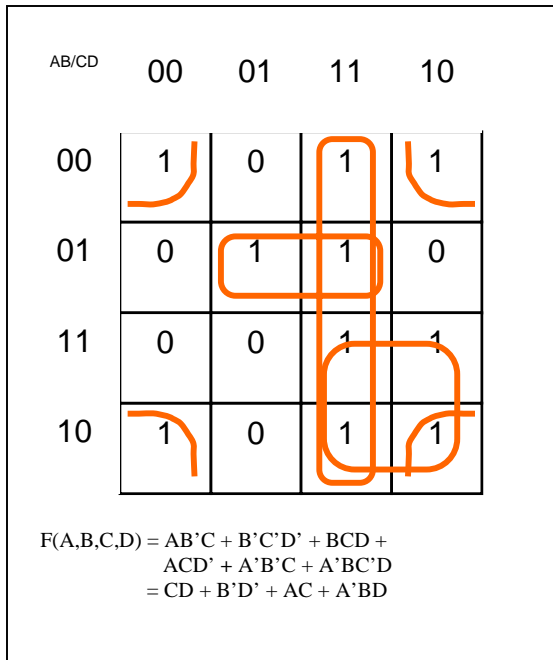
a)



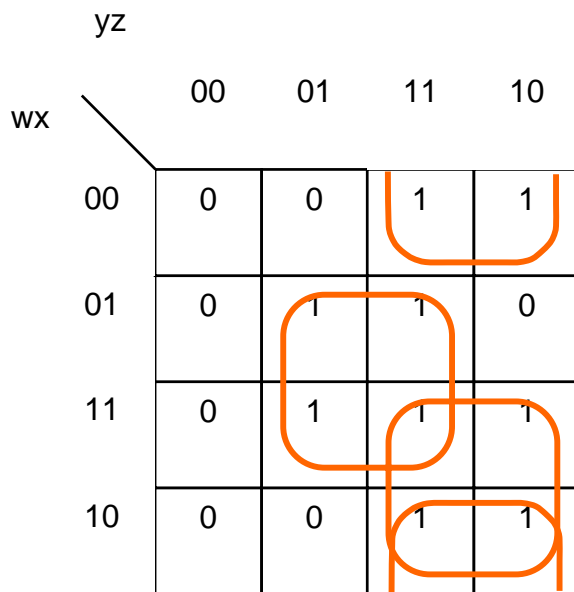
b)



c)



d)

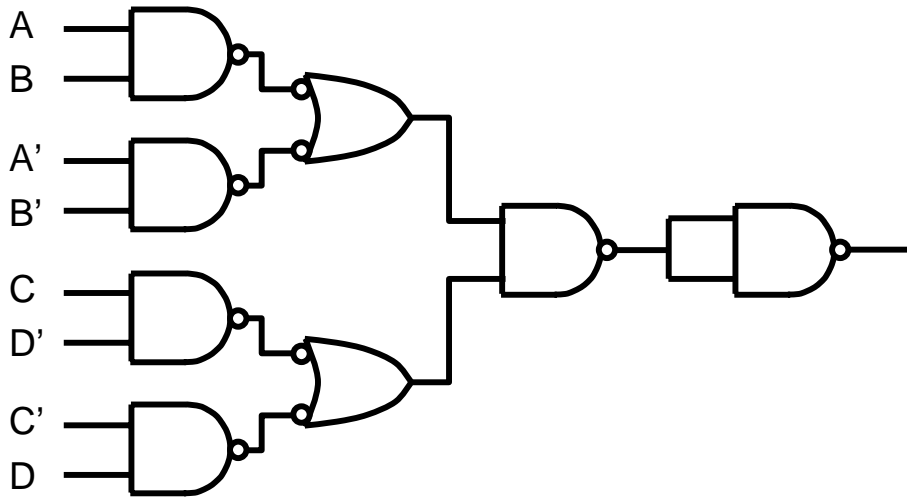
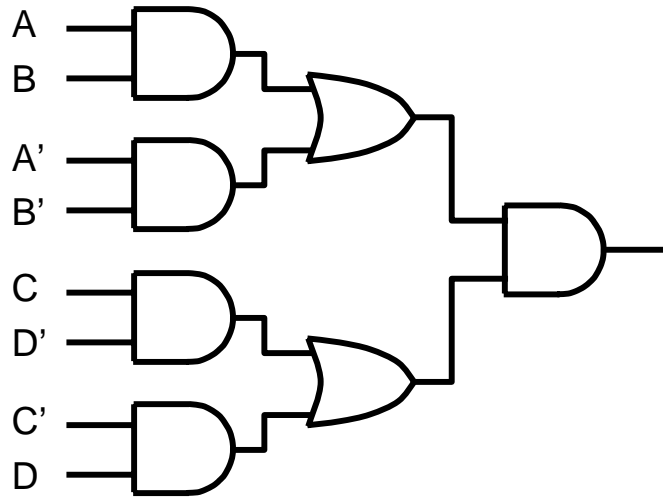


$$F(w,x,y,z) = wxy + yz + xy'z + x'y = xz + wy + x'y$$

3-18) Draw a logic diagram using only two-input NAND gates to implement the following expression:

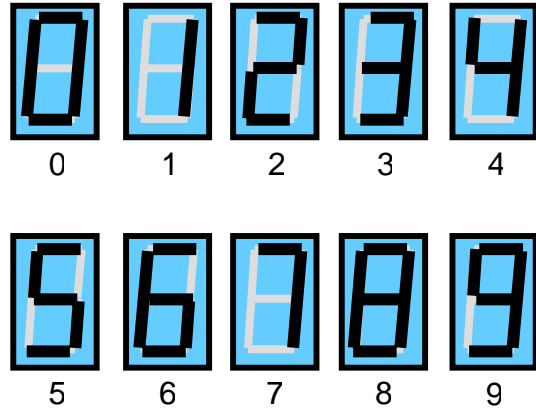
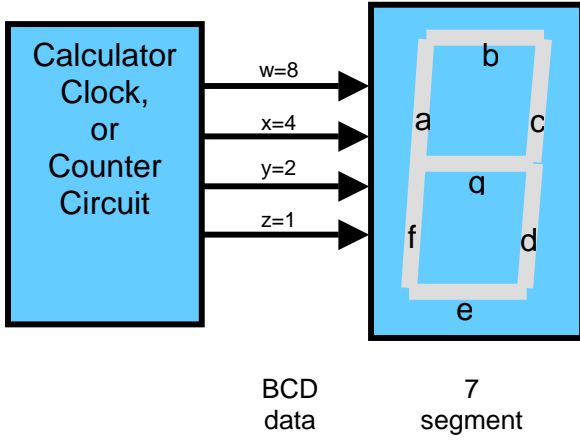
$$(AB + A'B')(CD' + C'D)$$

$$(AB + A'B')(CD' + C'D)$$



BCD to 7-segment decoder for segments a-f:

- a-
- b-
- c-
- d-
- e-
- f-



a:

wxlyz 00 01 11 10

00	1	0	0	0
01	1	1	0	1
11	X	X	X	X
10	1	1	X	X

$$F_a(w,x,y,z) = y'z' + xz' + xy' + w$$

wxlyz 00 01 11 10

00	1	0	0	0
01	1	1	0	1
11	X	X	X	X
10	1	1	X	X

$$F_a'(w,x,y,z) = w'x'y + w'x'z + yz$$

b:

wx\yz 00 01 11 10

00	1	0	1	1
01	0	1	1	1
11	X	X	X	X
10	1	1	X	X

$$F_b(w,x,y,z) = y + w + xz + x'z'$$

wx\yz 00 01 11 10

00	1	0	1	1
01	0	1	1	1
11	X	X	X	X
10	1	1	X	X

$$F_b'(w,x,y,z) = w'x'y'z + w'xy'z'$$

c:

wx\yz 00 01 11 10

00	1	1	1	1
01	1	0	1	0
11	X	X	X	X
10	1	1	X	X

$$F_c(w,x,y,z) = x' + w + y'z' + yz$$

wx\yz 00 01 11 10

00	1	1	1	1
01	1	0	1	0
11	X	X	X	X
10	1	1	X	X

$$F'_c(w,x,y,z) = xy'z + xyz'$$

d:

wx\yz 00 01 11 10

00	1	1	1	0
01	1	1	1	1
11	X	X	X	X
10	1	1	X	X

$$F_d(w,x,y,z) = x + y' + z$$

wx\yz 00 01 11 10

00	1	1	1	0
01	1	1	1	1
11	X	X	X	X
10	1	1	X	X

$$F_d'(w,x,y,z) = x'yz'$$

e:

wxyz	00	01	11	10
00	1	0	1	1
01	0	1	0	1
11	X	X	X	X
10	1	1	X	X

$$F_e(w,x,y,z) = w + x'y + yz' + x'y'z' + xy'z$$

wxyz	00	01	11	10
00	1	0	1	1
01	0	1	0	1
11	X	X	X	X
10	1	1	X	X

$$F_e'(w,x,y,z) = xy'z' + w'x'y'z + xyz$$

f: wx\yz 00 01 11 10

00	1	0	0	1
01	0	0	0	1
11	X	X	X	X
10	1	0	X	X

$$F_f(w,x,y,z) = x'z' + yz'$$

wx\yz 00 01 11 10

00	1	0	0	1
01	0	0	0	1
11	X	X	X	X
10	1	0	X	X

$$F_f'(w,x,y,z) = xy' + z$$