

Homework 1 – due 5/24/04

1-7) Express the following numbers in decimal:

$$(10110.0101)_2 = 22.3125,$$

$$(16.5)_{16} = (1\ 0110.0101)_2,$$

$$(26.24)_8 = (10\ 110.010\ 100)_2$$

$$(10110.0101)_2 = 2^4 + 2^2 + 2^1 + 2^{-2} + 2^{-4} = 16 + 4 + 2 + .25 + 0.0625 = 22.3125_{10}$$

$$(16.5)_{16} = (1\ 0110.0101)_2 = 22.3125_{10}$$

$$(26.24)_8 = (10\ 110.010\ 100)_2 = 22.3125_{10}$$

1-11) Do the following conversions:

a) $(34.4375)_{10}$ to binary = $(100010.0111)_2$

b) Calculate $(1/3)_{10}$ to 8 binary places. Convert result to decimal. How close is result to $(1/3)_{10}$?

c) Convert the binary result in (b) to hexadecimal, then convert to decimal. Is the answer the same?

$$(0.55)_{16} = 0.34375$$

a)

$$34.4375 = 34 + .4375$$

$$34 = 17 * 2 + 0$$

$$17 = 8 * 2 + 1$$

$$8 = 4 * 2 + 0$$

$$4 = 2 * 2 + 0$$

$$2 = 2 * 1 + 0$$

0

$$\text{result } 34_{10} = 100010_2$$

$$.4375 = .5 * 0 + .4375$$

$$.875 = .5 * 1 + .375$$

$$.75 = .5 * 1 + .25$$

$$.5 = .5 * 1 + 0$$

$$\text{result } .4375_{10} = 0.0111_2$$

$$\text{final result } 34.4375_{10} = 100010.0111_2$$

b)

divide 1/3 to 8 binary places:

$$\begin{array}{r} 0.01010101 \\ 11 \overline{) 1.00000000} \\ \underline{011} \\ 00100 \\ \underline{011} \\ 00100 \\ \underline{011} \\ 100 \\ \underline{11} \\ 1 \end{array}$$

Convert result to decimal:

$$0.01010101_2 = .25 + .0625 + .015625 + .00390625 = .33203125_{10}$$

$$\text{Difference} = 2^{-10} < .001302083 < 2^{-9}$$

c)

$$0.01010101_2 = 0.55_{16} = 5 * 16^{-1} + 5 * 16^{-2} = 5 * .0625 + 5 * .00390625 = .33203125 - \text{same result}$$

1-13) Perform the following division in binary 1011111/101

$$\begin{array}{r}
 \underline{00\ 10\ 01\ 1} \\
 101 \overline{) 10\ 11\ 11\ 1} \\
 \underline{10\ 1} \\
 01\ 11 \\
 \underline{1\ 01} \\
 \ 10\ 1 \\
 \underline{10\ 1} \\
 \ 0
 \end{array}$$

To check, perform the multiplication $10011 \cdot 101 = 1011111$

$$\begin{array}{r}
 11 \\
 \times \underline{1\ 01} \\
 11 \\
 \underline{1\ 00\ 11} \\
 1\ 01\ 11\ 11
 \end{array}$$

1-20) Convert decimal +61 and +27 to binary using the signed-2's complement representation and enough digits to accommodate the numbers. Then perform the binary equivalent of (+27) + (-61), (-27) + (+61) and (-27) + (-61). Convert the answers back to decimal and verify that they are correct.

$$\begin{aligned}
 61_{10} &= 32+16+8+4+1 = 111101_2 \\
 27_{10} &= 16+8+2+1 = 11011_2
 \end{aligned}$$

The sum (61 + 27) will exceed 64, so we need to represent numbers from -128 - +127, requiring 8 bits

$$\begin{aligned}
 +61_{10} &= 00111101_2 \\
 -61_{10} &= 11000011_2 \\
 +27_{10} &= 00011011_2 \\
 -27_{10} &= 11100101_2
 \end{aligned}$$

(+27) + (-61): -34

$$\begin{array}{r}
 \\
 \underline{+1100\ 0011} \\
 1101\ 1110 = -(0010\ 0001 + 1) = -(0010\ 0010) - (32 + 2) = -34
 \end{array}$$

(-27) + (+61): +34

$$\begin{array}{r}
 \\
 \underline{+0011\ 1101} \\
 (1)0010\ 0010 = (0010\ 0010) = +34
 \end{array}$$

(-27) + (-61): +88

$$\begin{array}{r}
 \\
 \underline{+1100\ 0011} \\
 (1)1010\ 1000 = -(0101\ 0111 + 1) = -(0101\ 1000) = -(64+16+8) = +88
 \end{array}$$